

# Airport Taxi Operations Modeling: GreenSim

John Shortle, Rajesh Ganesan, Liya Wang,  
Lance Sherry, Terry Thompson, C.H. Chen

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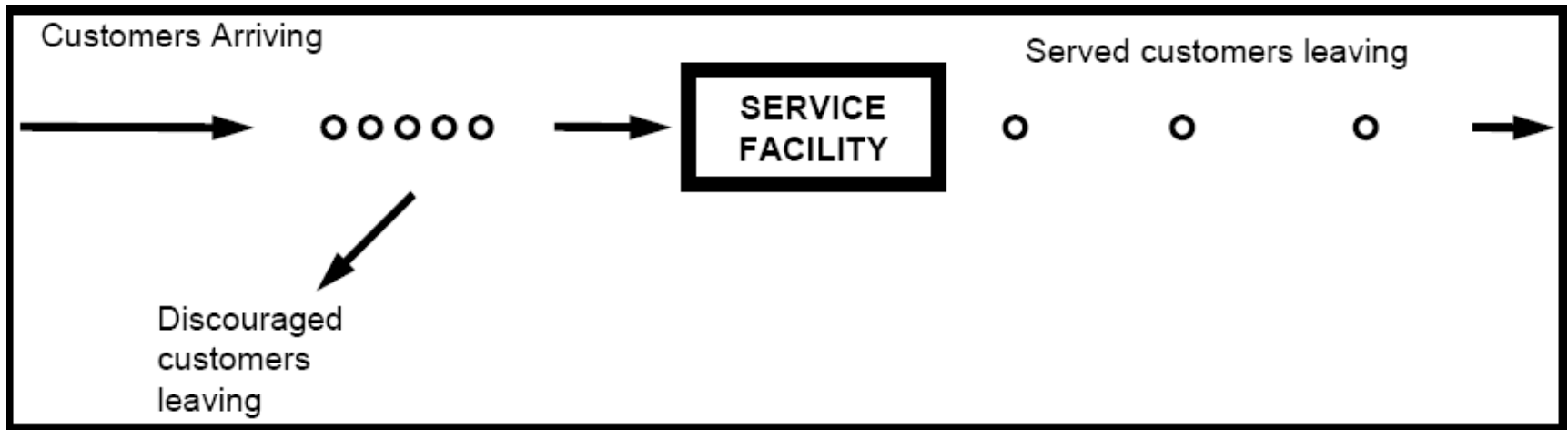
# Outline

- Queueing 101
- GreenSim: Modeling and Analysis
- Tool Demonstration & Case Study

# Motivation

- GreenSim
  - Airport as a “black-box”
    - 5 stage queueing model
  - Schedule and configuration dependent
    - Queueing models configured based on historic data
  - Stochastic behavior (i.e. Monte Carlo)
    - Behavior determined by distributions
  - Comparison of procedures (e.g. RNP procedures) and technologies (e.g. surface management)
    - Adjust distributions to reflect changes
  - Rapid (< 1 week)
    - Fast set-up and run

# Typical Queueing Process

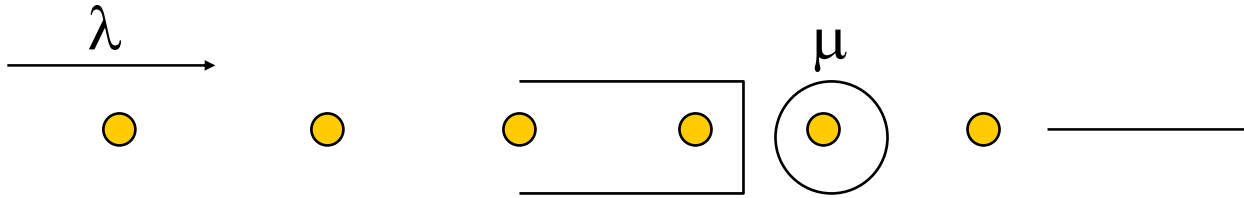


## Common Notation

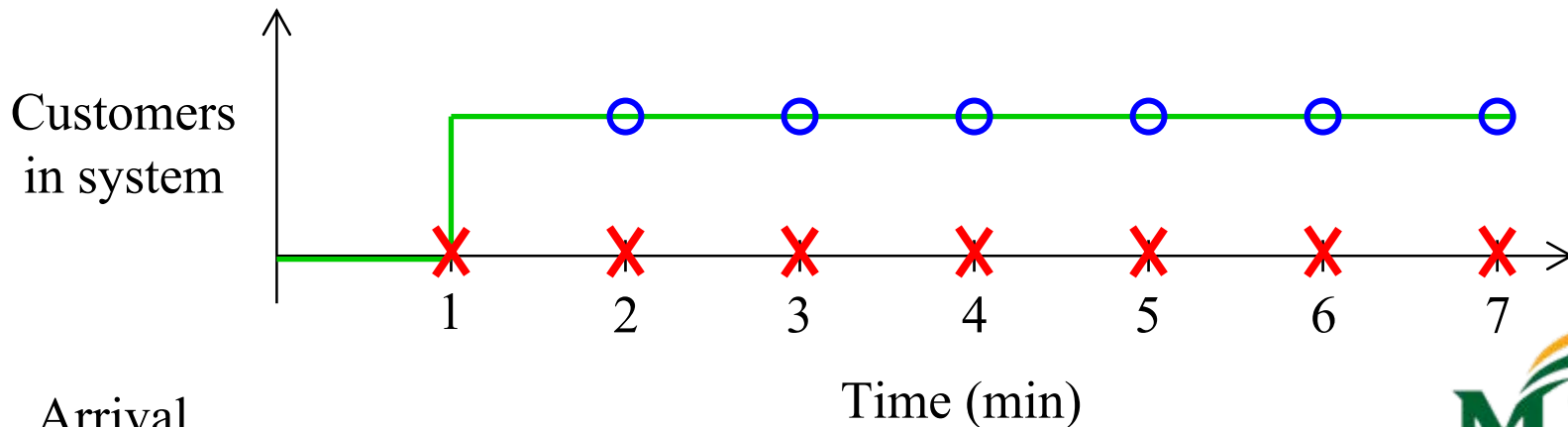
- $\lambda$ : Arrival Rate (e.g., customer arrivals per hour)
- $\mu$ : Service Rate (e.g., service completions per hour)
- $1/\mu$ : Expected time to complete service for one customer
- $\rho$ : Utilization:  $\rho = \lambda / \mu$



# A Simple Deterministic Queue



- Customers arrive at 1 min, 2 min, 3 min, etc.
- Service times are exactly 1 minute.
- What happens?

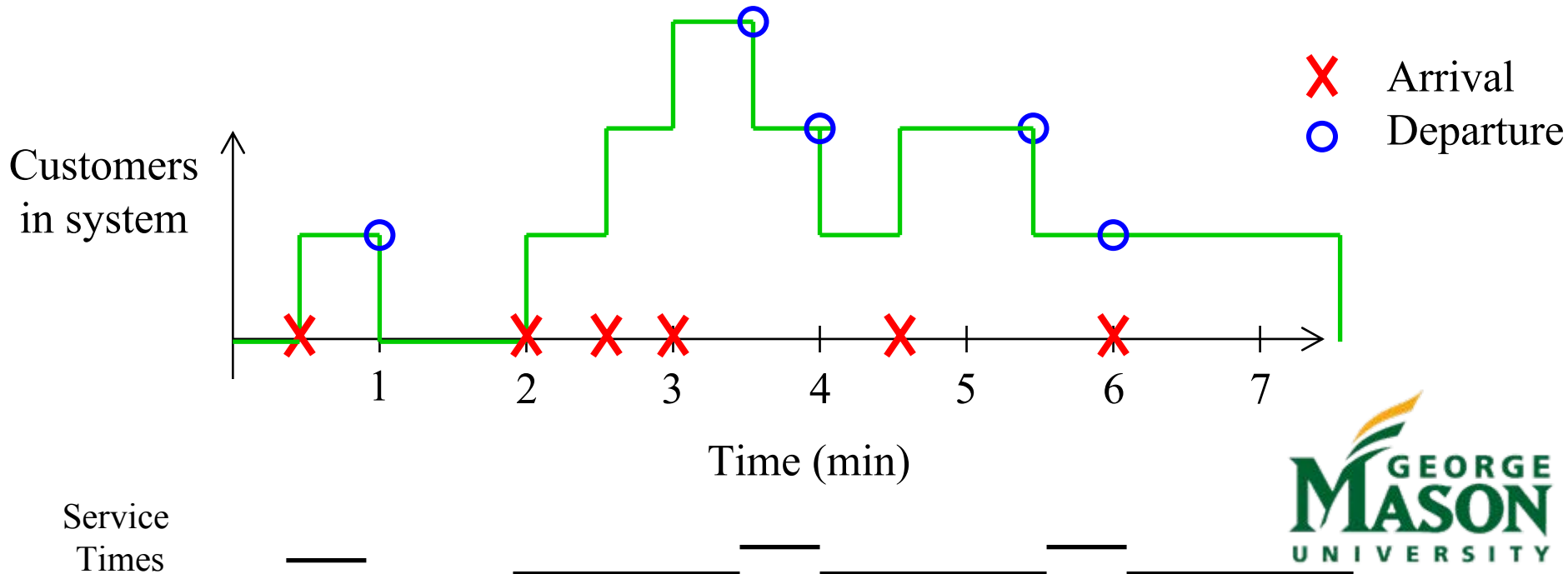


- ✗ Arrival
- Departure

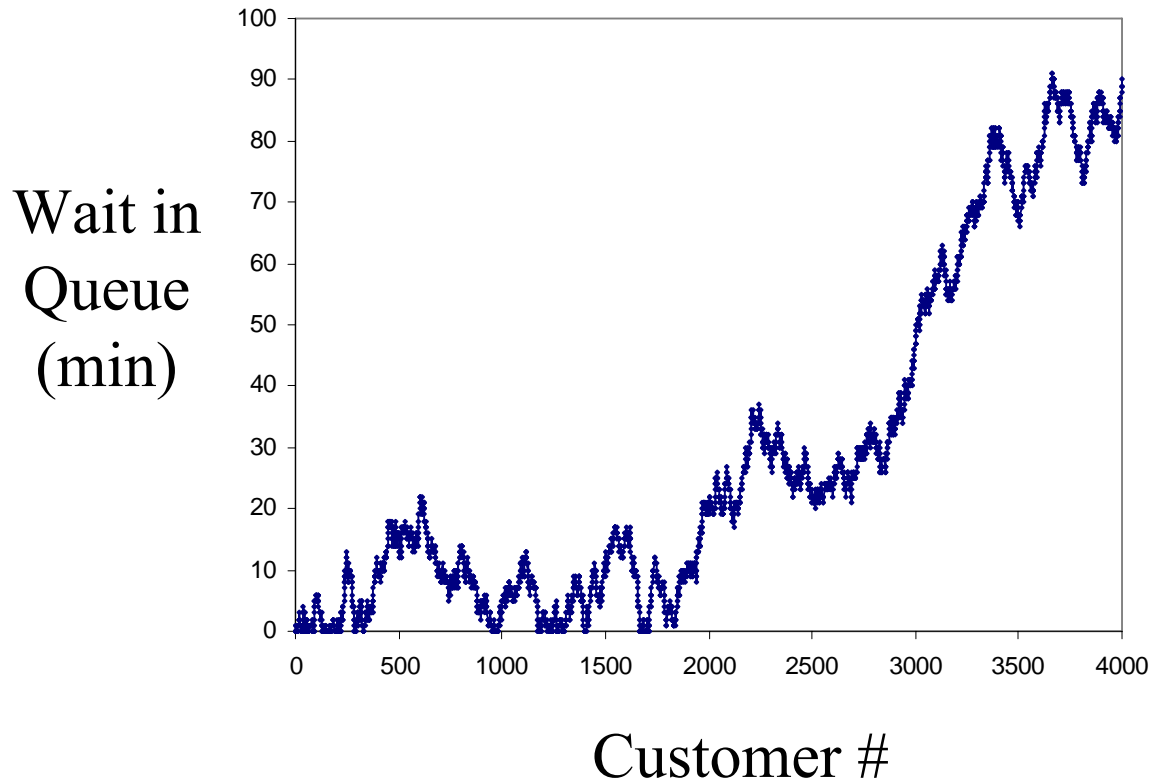


# A Stochastic Queue

- Times between arrivals are  $\frac{1}{2}$  min. or  $1\frac{1}{2}$  min. (50% each)
- Service times are  $\frac{1}{2}$  min. or  $1\frac{1}{2}$  min. (50% each)
- Average inter-arrival time = 1 minute
- Average service time = 1 minute
- What happens?



# Stochastic Queue in the Limit



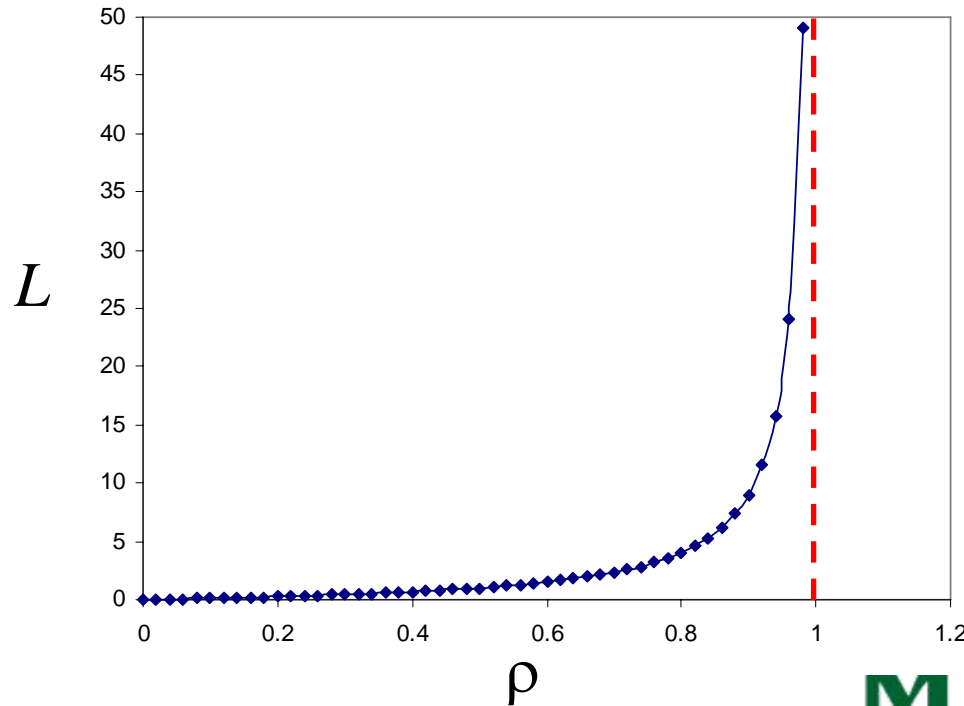
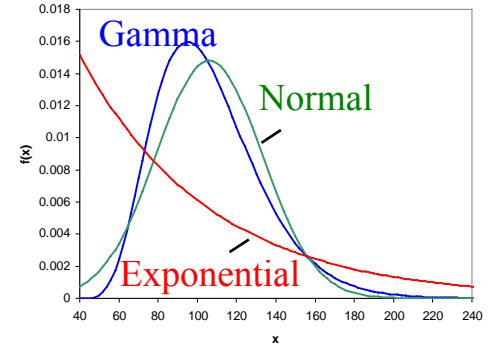
- Two queues with same average arrival and service rates
  - Deterministic queue: zero wait in queue for every customer
  - Stochastic queue: wait in queue grows without bound
- 7 • Variance is an enemy of queueing systems



# The $M/M/1$ Queue

Inter-arrival times follow an exponential distribution (or arrival process is Poisson)

A single server  
Service times follow an exponential distribution



$$L = \frac{\rho}{1 - \rho}$$

Avg. # in System

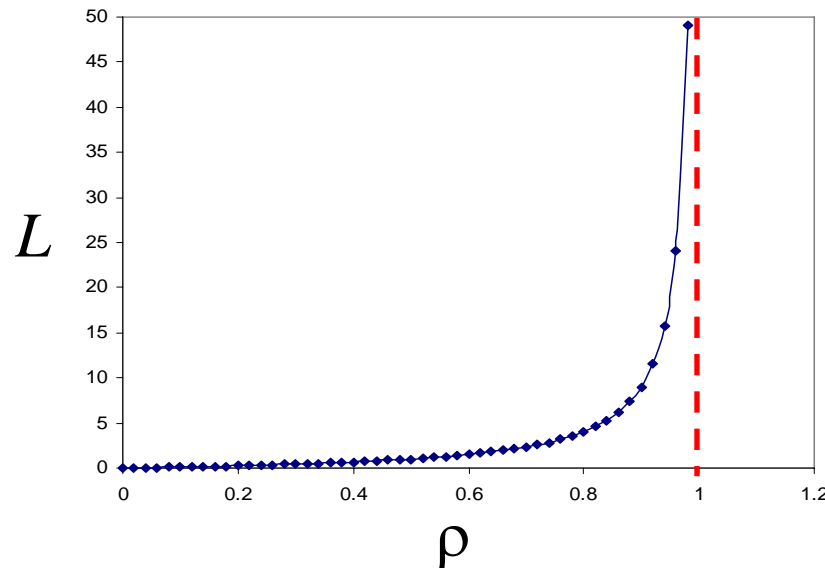




# The $M/M/1$ Queue

- Observations
  - 100% utilization is not desired
- Limitations
  - Model assumes steady-state. Solution does not exist when  $\rho > 1$  (arrival rate exceed service rate).
  - Poisson arrivals can be a reasonable assumption
  - Exponential service distribution is usually a bad assumption.

$$L = \frac{\rho}{1 - \rho}$$



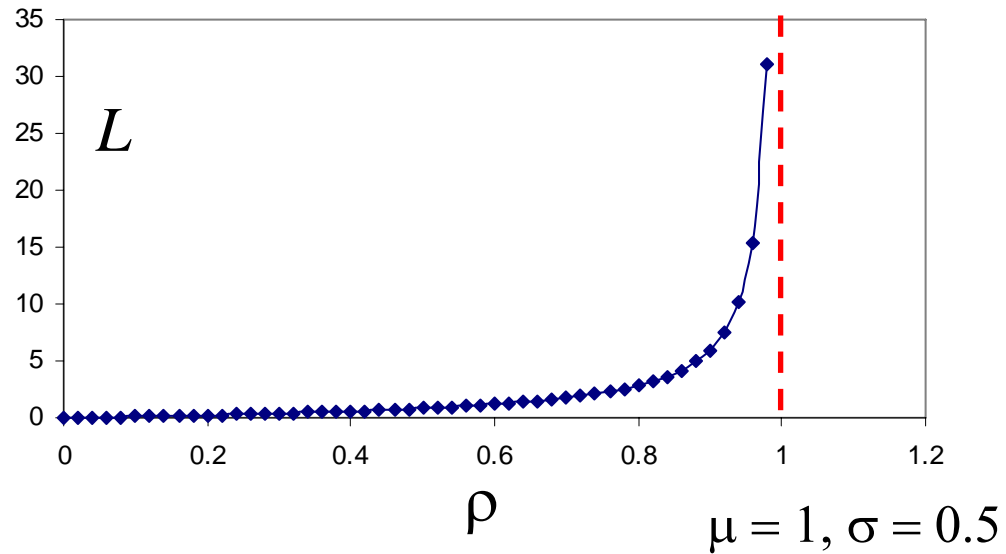


# The $M/G/1$ Queue

Service times follow a general distribution

Required inputs:

- $\lambda$ : arrival rate
- $1/\mu$ : expected service time
- $\sigma$ : std. dev. of service time

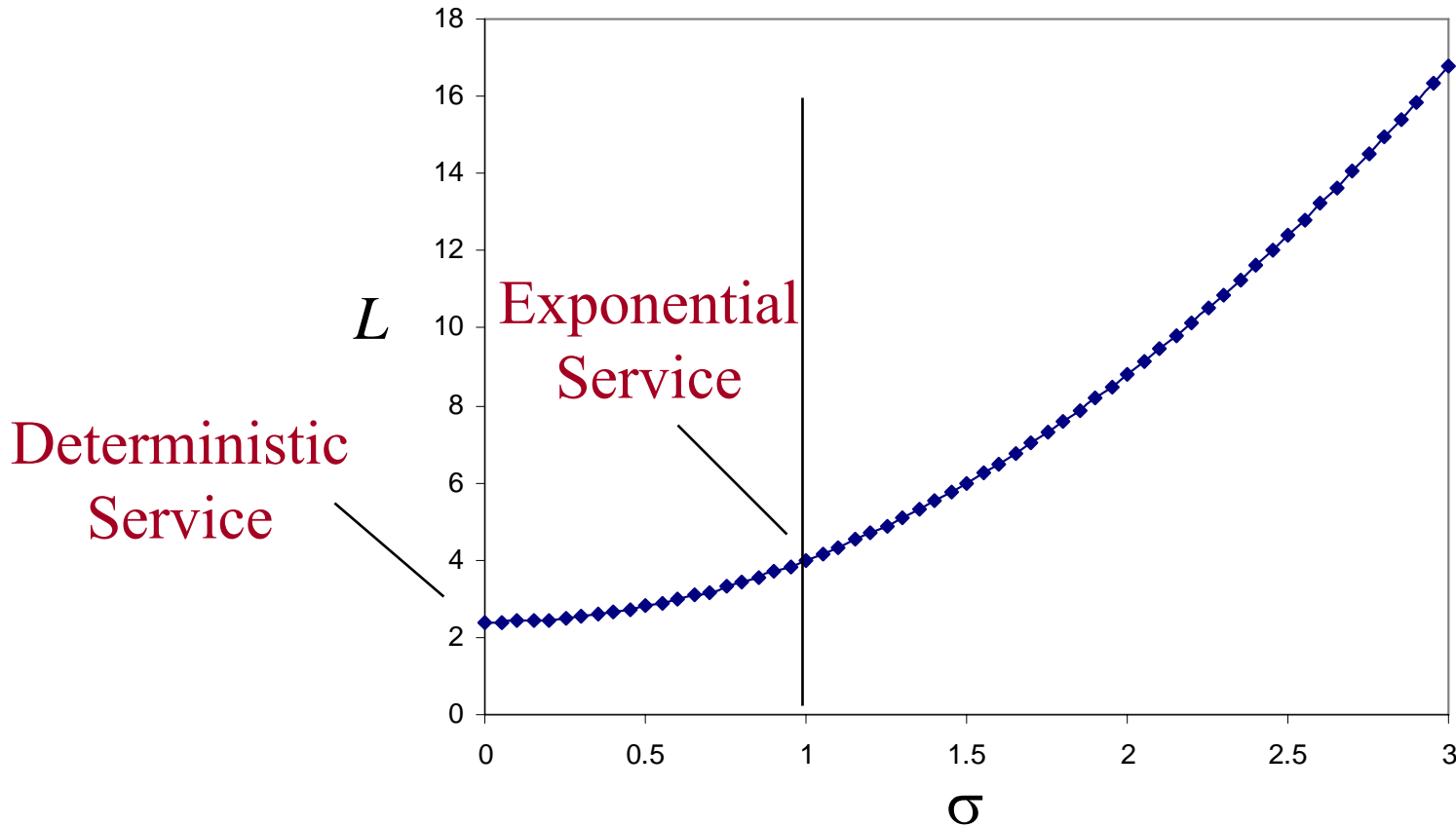


$$L = \rho + \frac{\rho^2 + \lambda^2 \sigma^2}{2(1 - \rho)}$$

Avg. # in System



# M/G/1: Effect of Variance



Arrival Rate  
Service Rate  
Held  
Constant

$$L = \rho + \frac{\rho^2 + \lambda^2 \sigma^2}{2(1 - \rho)}$$

$$\lambda = 0.8, \mu = 1 (\rho = 0.8)$$



# Other Queues

- $G/G/1$ 
  - No simple analytical formulas
  - Approximations exist
- $G/G/\infty$ 
  - Infinite number of servers – no wait in queue
  - Time in system = time in service
- $M(t)/M(t)/1$ 
  - Arrival rate and service rate vary in time
  - Arrival rate can be temporarily bigger than service rate

# Queueing Theory Summary

- Strengths
  - Demonstrates basic relationships between delay and statistical properties of arrival and service processes
  - Quantifies cost of variability in the process
  - Analytical models easy to compute
- Potential abuses
  - Only simple models are analytically tractable
  - Analytical formulas generally assume steady-state
  - Theoretical models can predict exceptionally high delays
  - Correlation in arrival process often ignored
- Simulation can be used to overcome limitations

# GreenSim



CATSR



Java Airport Simulation Software

Airport : **BWI**

From : 8/1/2005

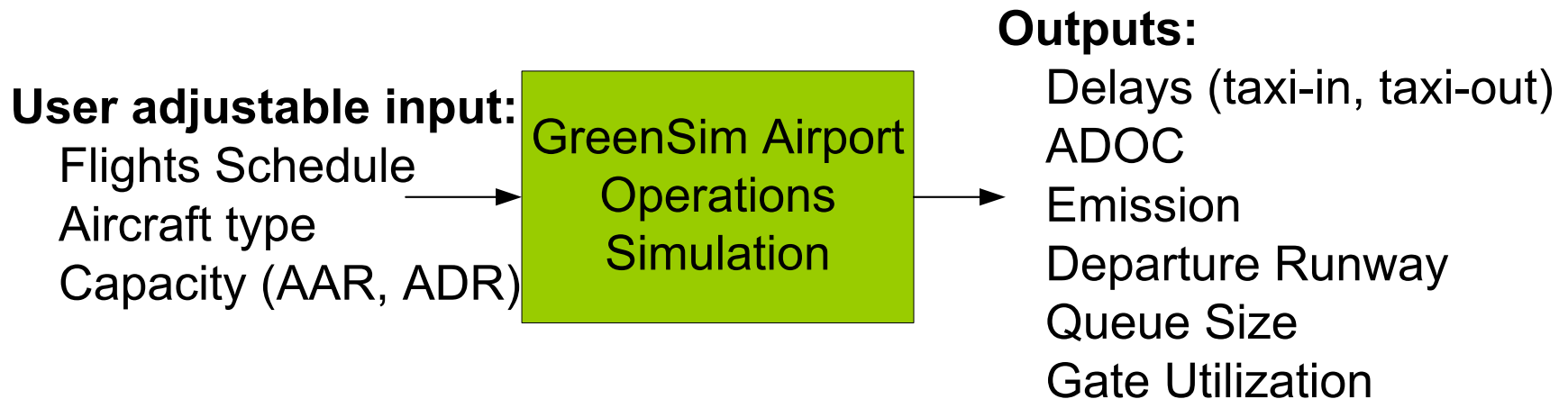
To : 8/1/2005

**Demand and Capacity Input**

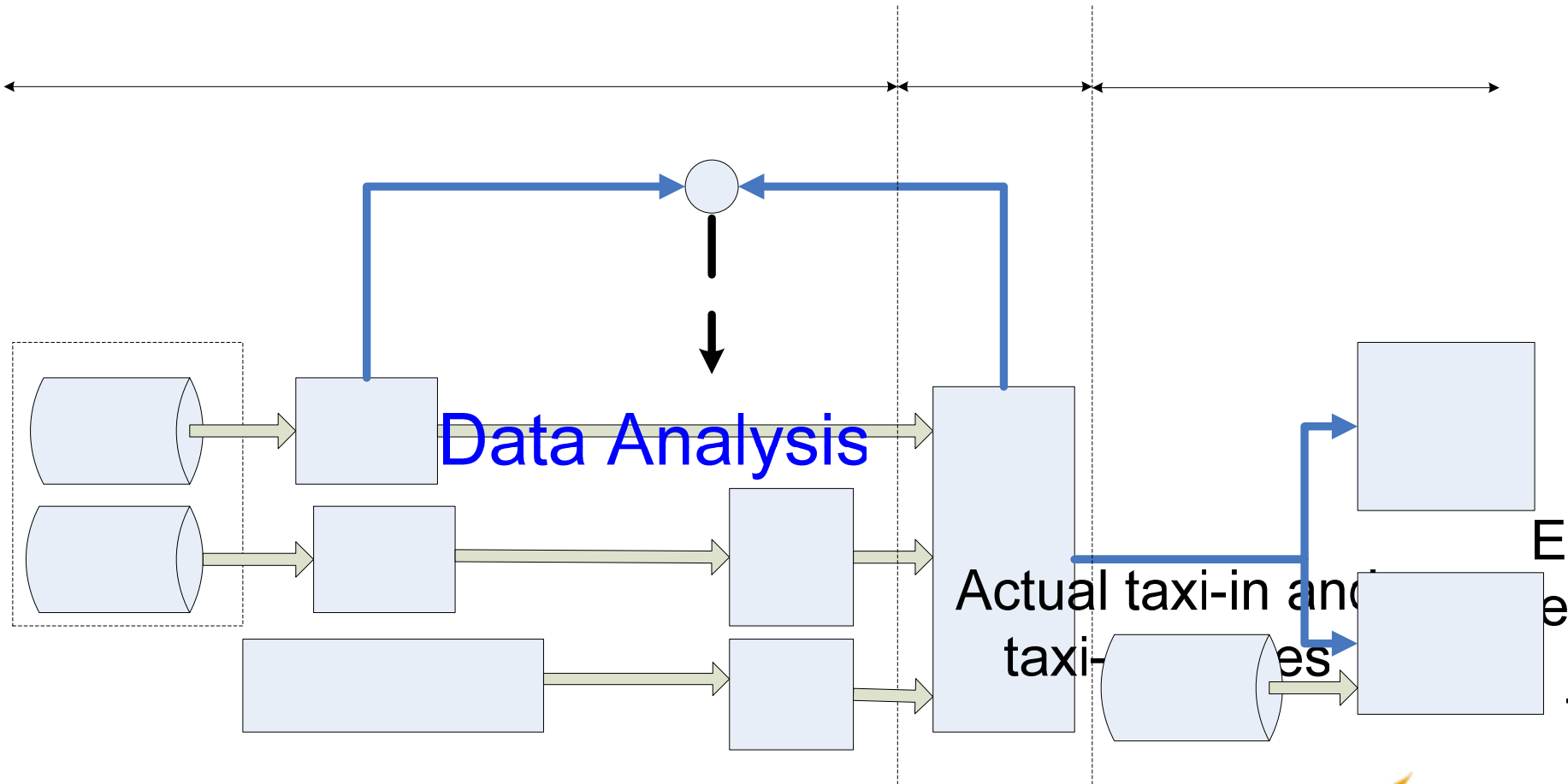
- Input Report
- Input Graphs
- Fleet Mix
- Service Time Setting
- Run Simulation
- Output Graphs
- Output Report
- Emission Calculation
- Exit



# GreenSim Input/Output Model



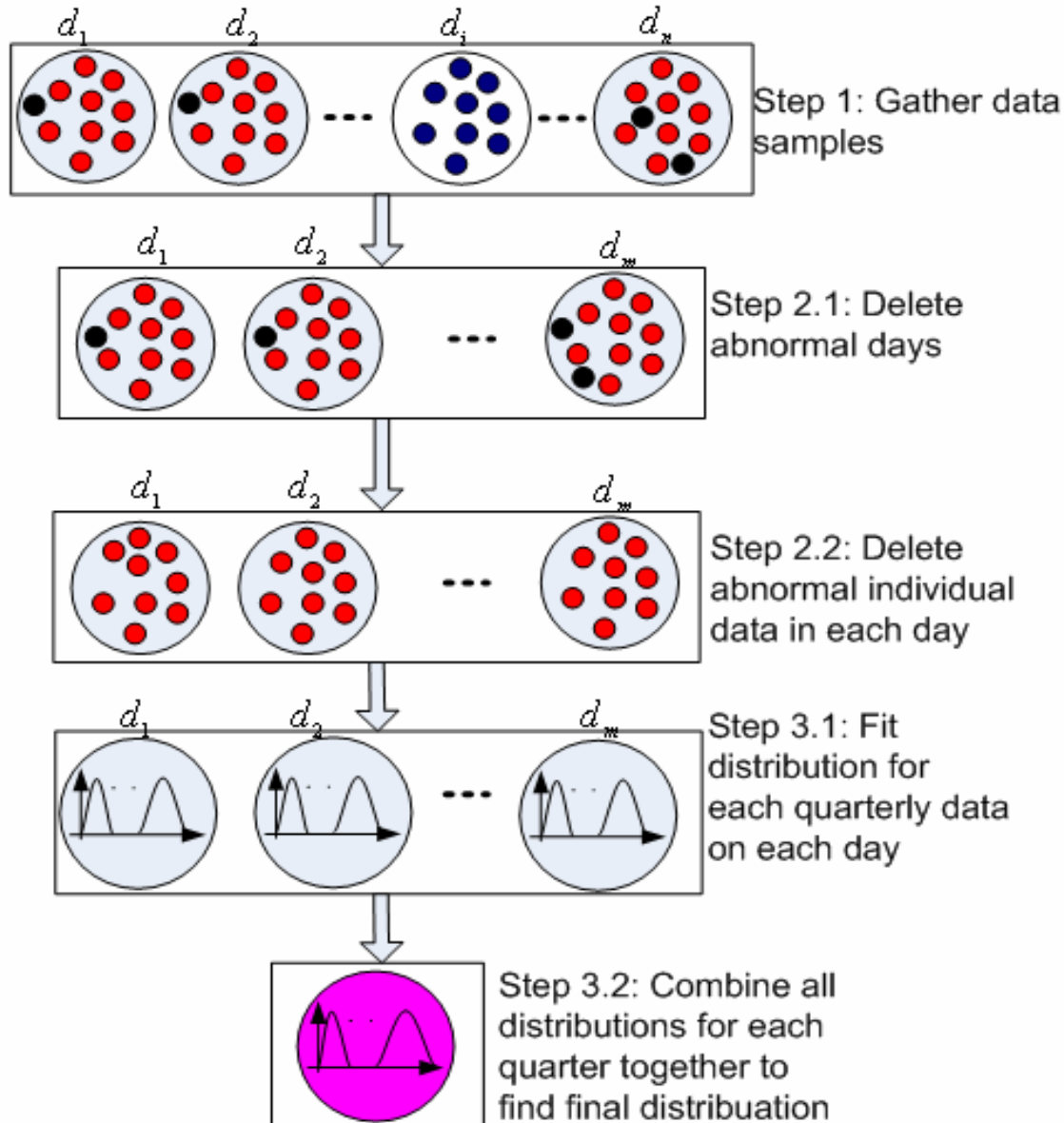
# GreenSim Architecture



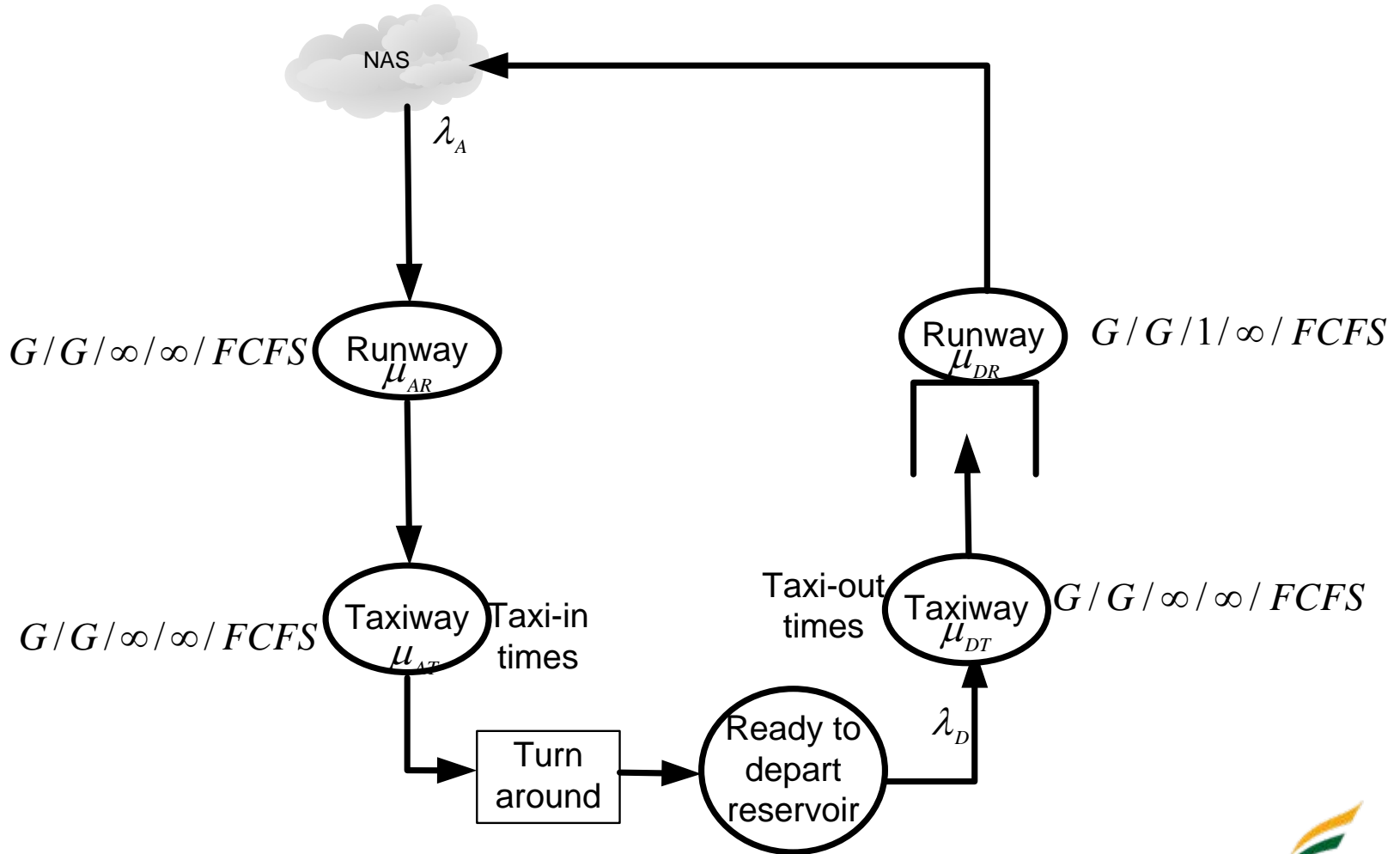




# Data Analysis Process



# Queueing Simulation Model



# Service Times Settings

Segment Name	Settings	Notation
Arrival Runway	$S1 \sim \text{Exponential}(1/\text{AAR})$	
Arrival Taxiway	$S2 \sim \text{NOMTI} + \text{DLATI} - S1$	$\text{DLATI} \sim \text{Normal}(u_1, \sigma_1)$
Departure Taxiway	$S3 \sim \text{NOMTO} + \text{DLATO} - S4$	$\text{DLATO} \sim \text{Normal}(u_2, \sigma_2)$
Departure Runway	$S4 \sim \text{Exponential}(1/\text{ADR})$	



# Performance Analysis

- Delays (individual, quarterly average, hourly average, daily average)
- Fuel  $Fuel = \sum_j (TIM_j) \times (FF_j / 1000) \times (NE_j)$
- Emission (HC, CO, NOx, SOx)

$$Emission_i = \sum_j (TIM_j) \times (FF_j / 1000) \times (NE_j) \times EI_{ij}$$

$TIM_j$  = taxi time for type- $j$  aircraft  
 $FF_j$  = fuel flow per time per engine for type- $j$  aircraft  
 $NE_j$  = number of engines used for type- $j$  aircraft  
 $EI_{ij}$  = emissions of pollutant  $i$  per unit fuel consumed for type- $j$  aircraft



# EWR Hourly Average Delays

### Taxi-in Hourly Average Delays Comparison



### Taxi-out Hourly Average Delays Comparison

